

因数分解しなさい

$$x^3 - (a^2 - a + 1)x - a^2 + a$$

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$$\begin{aligned}& x^3 - (a^2 - a + 1)x - a^2 + a \\&= x^3 - a^2x + ax - x - a^2 + a \\&= -xa^2 - a^2 + ax + a + x^3 - x && \text{最低次数の } a \text{ で整理} \\&= (-x-1)a^2 + (x+1)a + x^3 - x \\&= -(x+1)a^2 + (x+1)a + x(x^2-1) \\&= -(x+1)a^2 + (x+1)a + x(x+1)(x-1) \\&= -(x+1)\left(a^2 - a - x(x-1)\right)\end{aligned}$$

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$$= -(x+1) \left(a^2 \overset{\text{aで、たすきがけ}}{-1}a - x(x-1) \right)$$

1	$\swarrow$	$-x$	$\longrightarrow$	$-x$
1	$\searrow$	$x-1$	$\longrightarrow$	$x-1$
				-1

$$= -(x+1)(a-x)(a+x-1) \quad \boxed{\text{答}}$$

$$-(a-x) = x-a$$

$$= (x+1)(x-a)(x+a-1) \quad \boxed{\text{答}}$$