

# 三角関数の性質

$$\sin(\theta + 2\pi) = \sin \theta$$

$$\cos(\theta + 2\pi) = \cos \theta$$

$$\tan(\theta + 2\pi) = \tan \theta$$

$$\sin(-\theta) = -\sin \theta$$

$$\cos(-\theta) = \cos \theta$$

$$\tan(-\theta) = -\tan \theta$$

$$\sin(\theta + \pi) = -\sin \theta$$

$$\cos(\theta + \pi) = -\cos \theta$$

$$\tan(\theta + \pi) = \tan \theta$$

$$\sin(\pi - \theta) = \sin \theta$$

$$\cos(\pi - \theta) = -\cos \theta$$

$$\tan(\pi - \theta) = -\tan \theta$$

$$\sin\left(\theta + \frac{\pi}{2}\right) = \cos \theta$$

$$\cos\left(\theta + \frac{\pi}{2}\right) = -\sin \theta$$

$$\tan\left(\theta + \frac{\pi}{2}\right) = -\frac{1}{\tan \theta}$$

$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$$

$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$

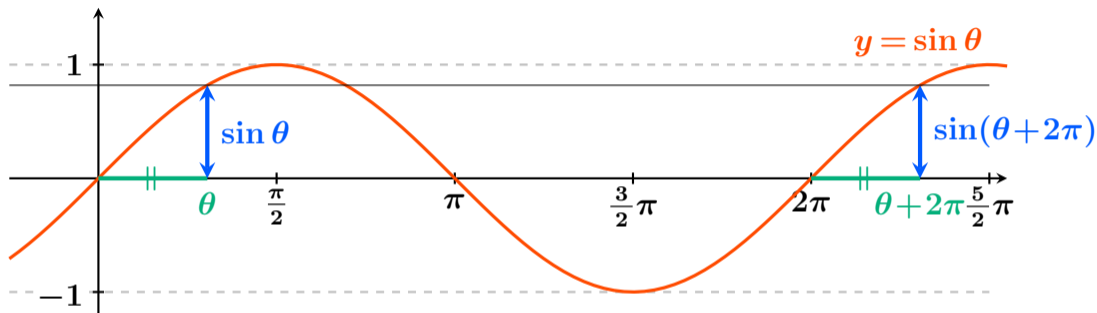
$$\tan\left(\frac{\pi}{2} - \theta\right) = \frac{1}{\tan \theta}$$

## 暗記する必要はないと思うよ…

そこまで重要な式だとは思わない。

しかし、これらの式が必要になったときはグラフの概形と対称性を使って式を導き出せるようになっておくことは必要だと思う。

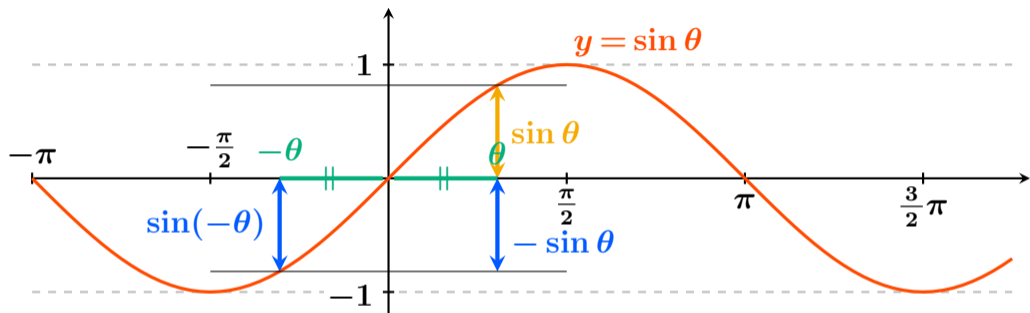
$$\sin(\theta + 2\pi) = \sin \theta$$



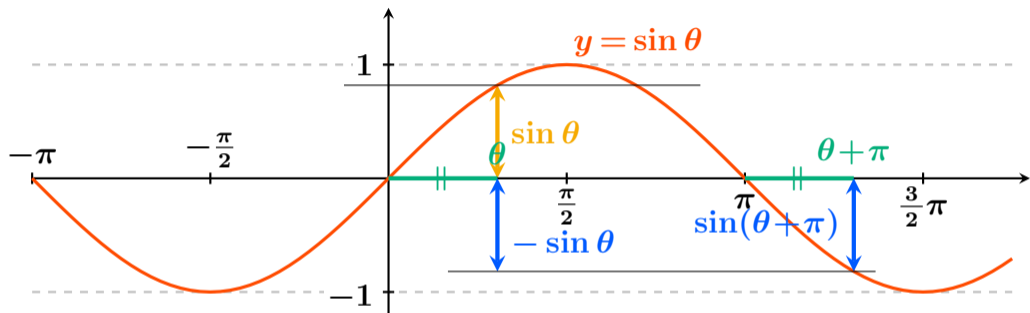
周期 $2\pi$ なので  $\sin(\theta + 4\pi) = \sin \theta$ ,  $\sin(\theta + 6\pi) = \sin \theta$  なども成り立つから

$$\text{まとめて} \quad \sin(\theta + 2n\pi) = \sin \theta$$

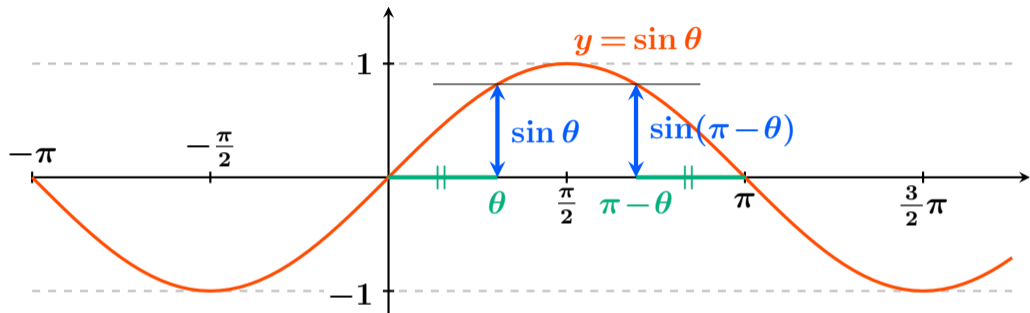
$$\sin(-\theta) = -\sin \theta$$



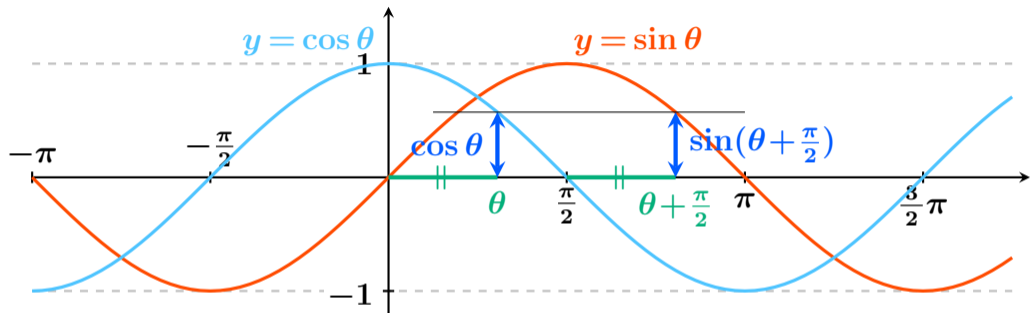
$$\sin(\theta + \pi) = -\sin \theta$$



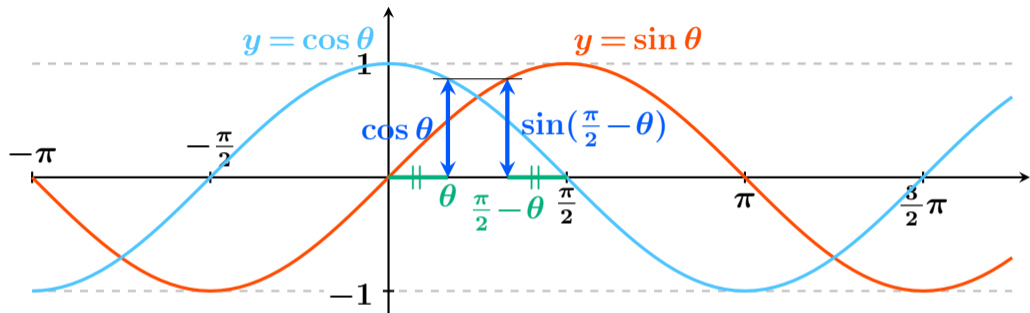
$$\sin(\pi - \theta) = \sin \theta$$



$$\sin\left(\theta + \frac{\pi}{2}\right) = \cos \theta$$

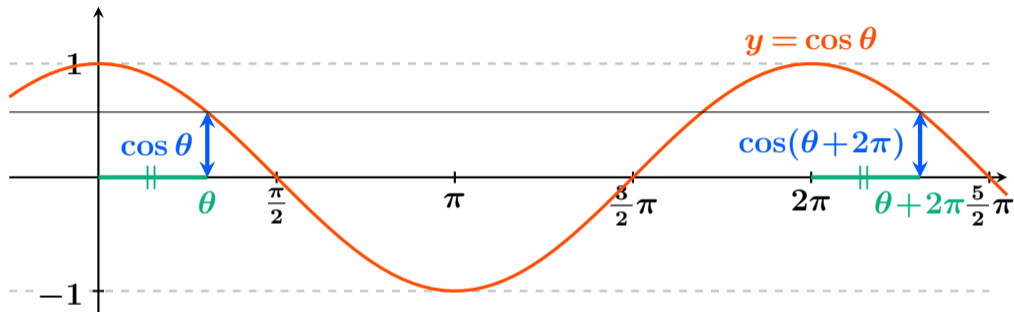


$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$$





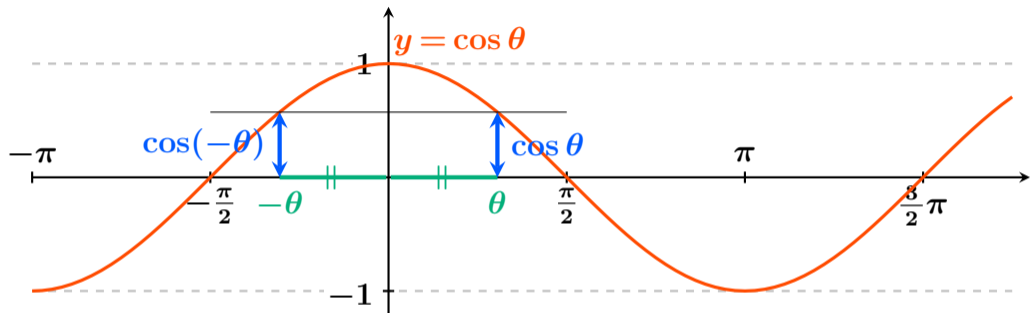
$$\cos(\theta + 2\pi) = \cos \theta$$



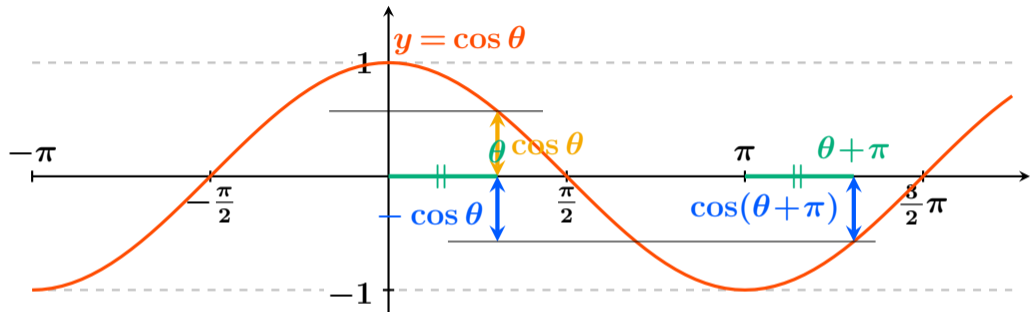
周期 $2\pi$ なので  $\cos(\theta + 4\pi) = \cos \theta$ ,  $\cos(\theta + 6\pi) = \cos \theta$  なども成り立つから

まとめて  $\cos(\theta + 2n\pi) = \cos \theta$

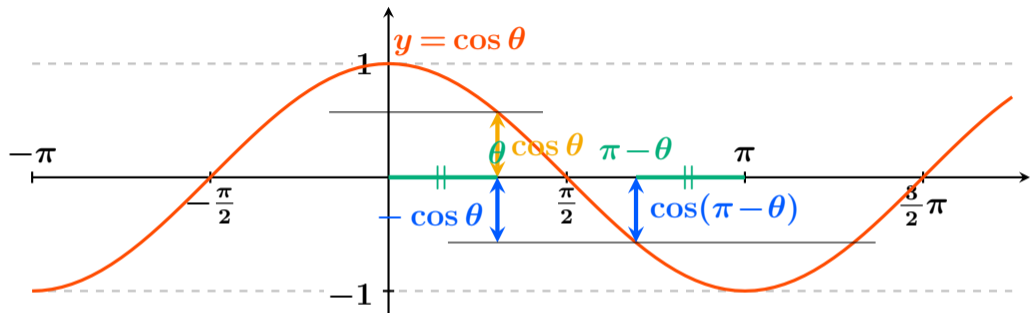
$$\cos(-\theta) = \cos \theta$$



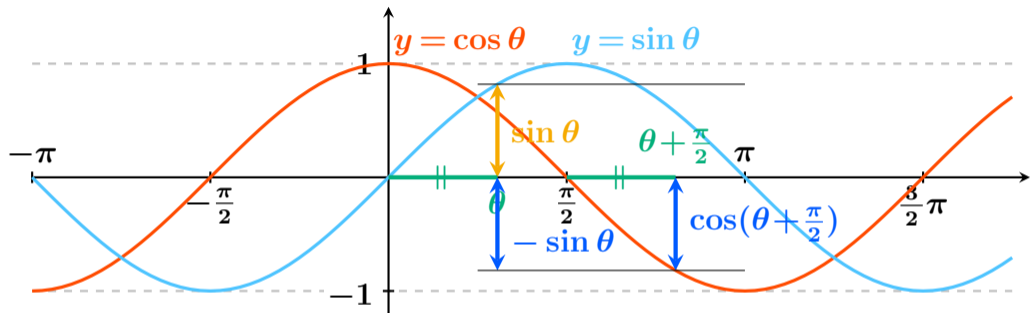
$$\cos(\theta + \pi) = -\cos \theta$$



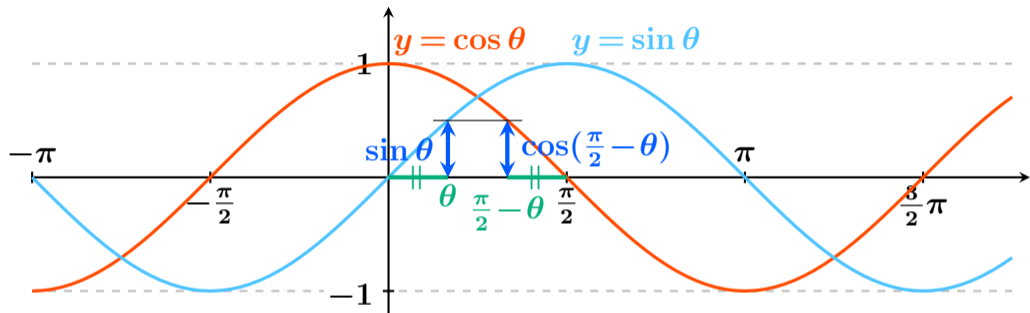
$$\cos(\pi - \theta) = -\cos \theta$$



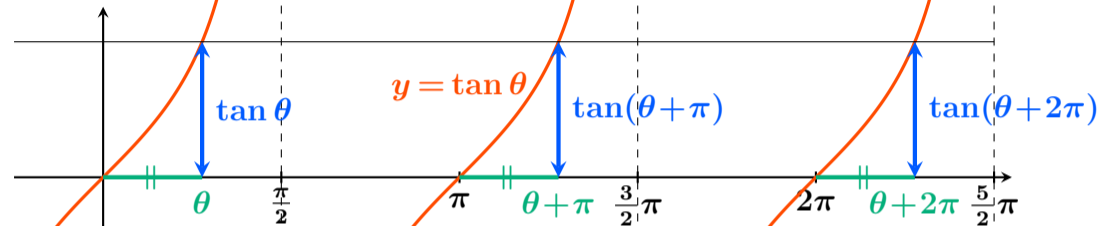
$$\cos\left(\theta + \frac{\pi}{2}\right) = -\sin \theta$$



$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$



$$\tan(\theta + 2\pi) = \tan \theta$$

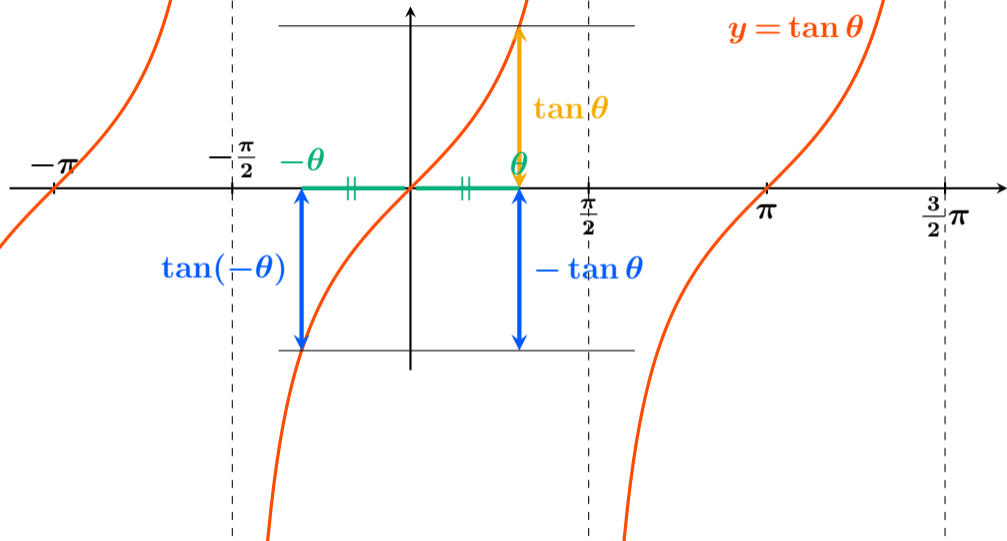


周期 $\pi$ なので  $\tan(\theta + 3\pi) = \tan \theta$ ,  $\tan(\theta + 4\pi) = \tan \theta$  なども成り立つから

まとめて

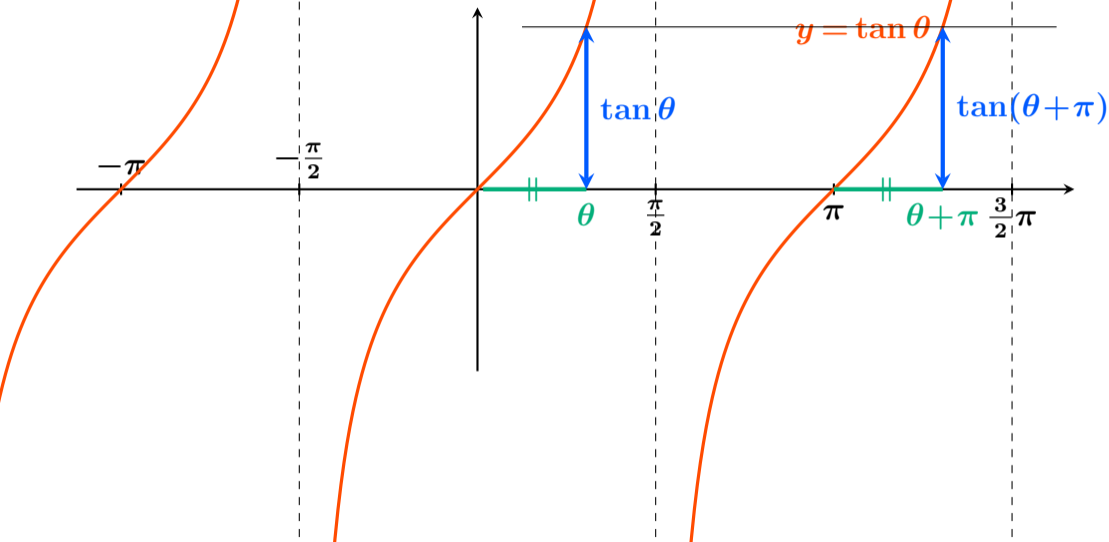
$$\tan(\theta + 2n\pi) = \tan \theta$$
$$\tan(\theta + n\pi) = \tan \theta$$

$$\tan(-\theta) = -\tan \theta$$

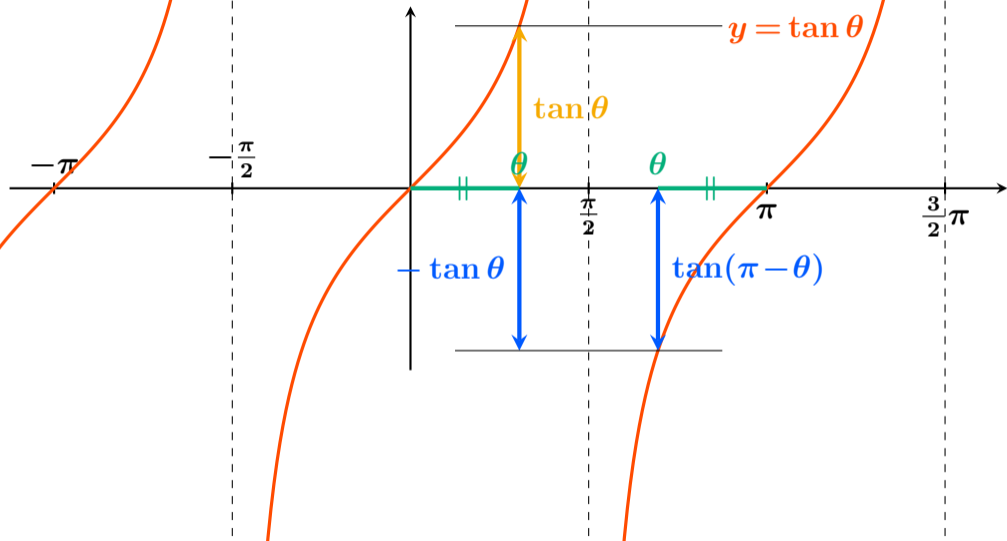




$$\tan(\theta + \pi) = \tan \theta$$

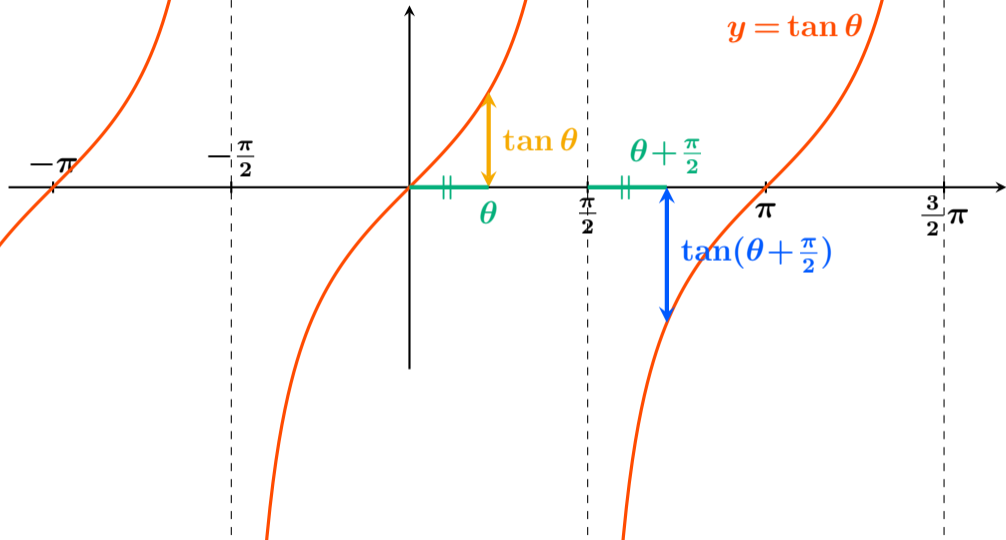


$$\tan(\pi - \theta) = -\tan \theta$$



$$\tan\left(\theta + \frac{\pi}{2}\right) = -\frac{1}{\tan \theta}$$

$y = \tan \theta$



$$\tan\left(\frac{\pi}{2} - \theta\right) = \frac{1}{\tan \theta}$$

